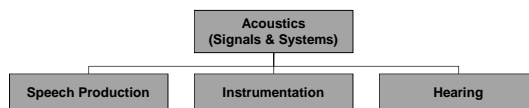


Acoustics of Speech and Hearing

Lecture 5
Frequency Response

Acoustics



- Week 2 – waveform, decibel
- Week 3 – period, frequency, sinewave
- Week 4 – fundamental frequency, harmonic, spectrum
- Week 5 – frequency response

Signals Review

- Classification
 - Simple & complex periodic waveforms
 - Impulsive & noise aperiodic waveforms
- Spectral analysis
 - Complex periodic waveforms analysed into a sum of harmonics (sinewaves at multiples of fundamental frequency)
 - Spectrum shows which sinewaves to add together to make waveform

Signals Review

- Loudness
 - related logarithmically to intensity
- Pitch
 - related to fundamental frequency
- Timbre
 - related to amplitude of harmonics (for complex periodic waveforms)

Overview

- Signals and systems
- How can we measure systems?
- Frequency response graph
- Frequency response of a simple resonator

Signals & Systems



- Signal
 - physical form of a waveform
 - e.g. sound, electrical current, radio wave
- System
 - a channel that changes a signal that passes through it
 - e.g. a telephone connection, a room, a vocal tract



Simple Systems

- A piece of wire
 - does nothing! \Rightarrow $\times 1.0$ \Rightarrow
- An amplifier
 - increases amplitude \Rightarrow $\times 10.0$ \Rightarrow
- An attenuator
 - decreases amplitude \Rightarrow $\times 0.1$ \Rightarrow
- BUT A simple resonator
 - does what to a signal? \Rightarrow $?$ \Rightarrow

Pulse into Simple Resonator

- Input Signal (Pulse) \Rightarrow $?$ \Rightarrow
- 
- Output Signal (Damped Sinusoid)
- 

Sinewaves into Simple Resonator

Response to Sinusoids \Rightarrow $?$ \Rightarrow

Description	Input	Output
Sinewave below natural frequency		
Sinewave at natural frequency		
Sinewave above natural frequency		

Define "Response"

- Mathematical expression of change of amplitude

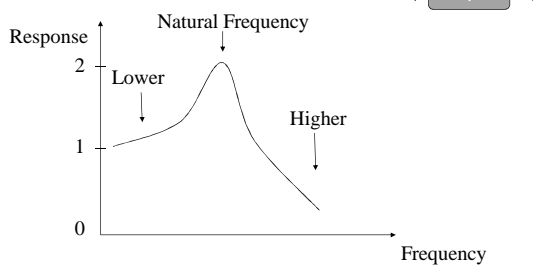
$$\text{Response} = \frac{\text{Output Amplitude}}{\text{Input Amplitude}}$$



- Usually expressed in decibels

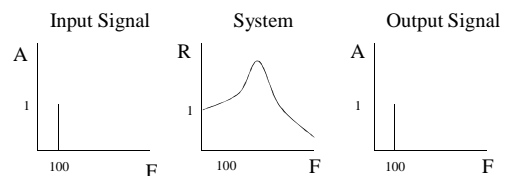
$$\text{Response (dB)} = 20 \log_{10} \left(\frac{\text{Output Amplitude}}{\text{Input Amplitude}} \right)$$

Simple Resonator Response



Frequency Response Graph

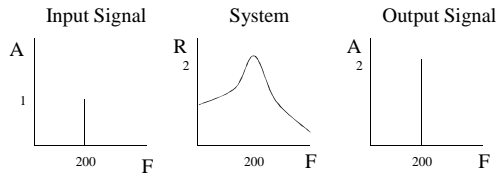
Frequency Domain Description



$$\text{Output} = \text{Input} \times \text{Response}$$

Frequency Response Graph

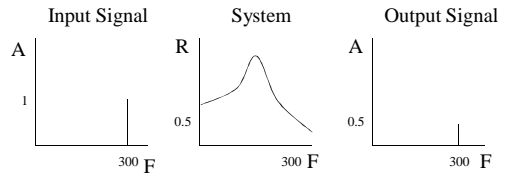
Frequency Domain Description



Output = Input × Response

Frequency Response Graph

Frequency Domain Description



Output = Input × Response

Frequency Response Graph

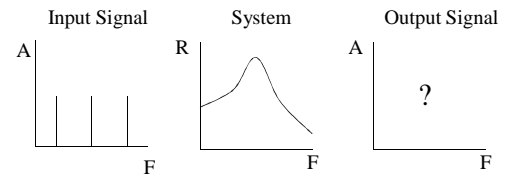
- Shows how *response* of a system to sinewaves varies as a function of frequency
- But can use to characterise how a system changes **any** signal **since any signal can be considered a sum of sinewaves!**

$$\text{Output amplitude} = \text{Input amplitude} \times \text{Response}$$

$$\text{Output spectrum} = \text{Input spectrum} \times \text{Frequency response}$$

Frequency Response Graph

Frequency Domain Description

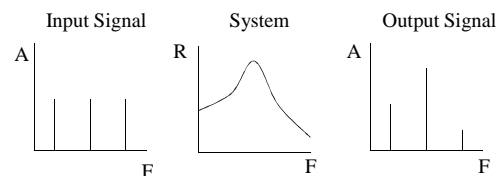


Input × Response = Output

⇒ Frequency Response ⇒

Frequency Response Graph

Frequency Domain Description



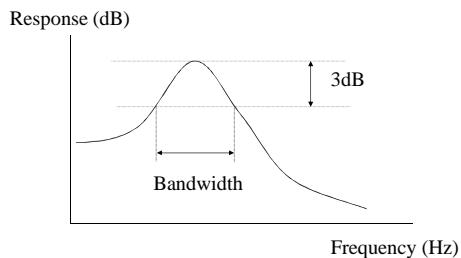
Input × Response = Output

⇒ Frequency Response ⇒

What about Damping?

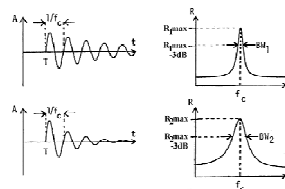
- We can measure the resonant frequency from the frequency response graph
 - as frequency of peak
- In fact we can also measure the amount of damping
 - as “peakiness” of peak
- Measure of “peakiness” is called **Bandwidth**

Bandwidth



Bandwidth & Damping

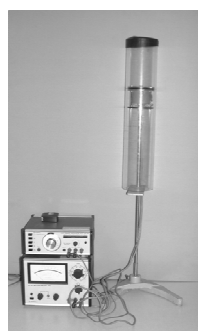
- Two ways of describing the same thing:
 - **Narrow** Bandwidth = **Low** Damping
 - **Wide** Bandwidth = **High** Damping



Summary

- Systems are channels that change signals that pass through them
- Response is an expression of the change in amplitude caused by system
- A **frequency response graph** shows how the system response varies with frequency (of sinewave input signals)
- A simple resonator has parameters of resonant frequency and bandwidth

Lab Experiment



- Measure the frequency response of the acoustic resonator for two lengths
- Increase damping and measure the effect of damping on the frequency response